

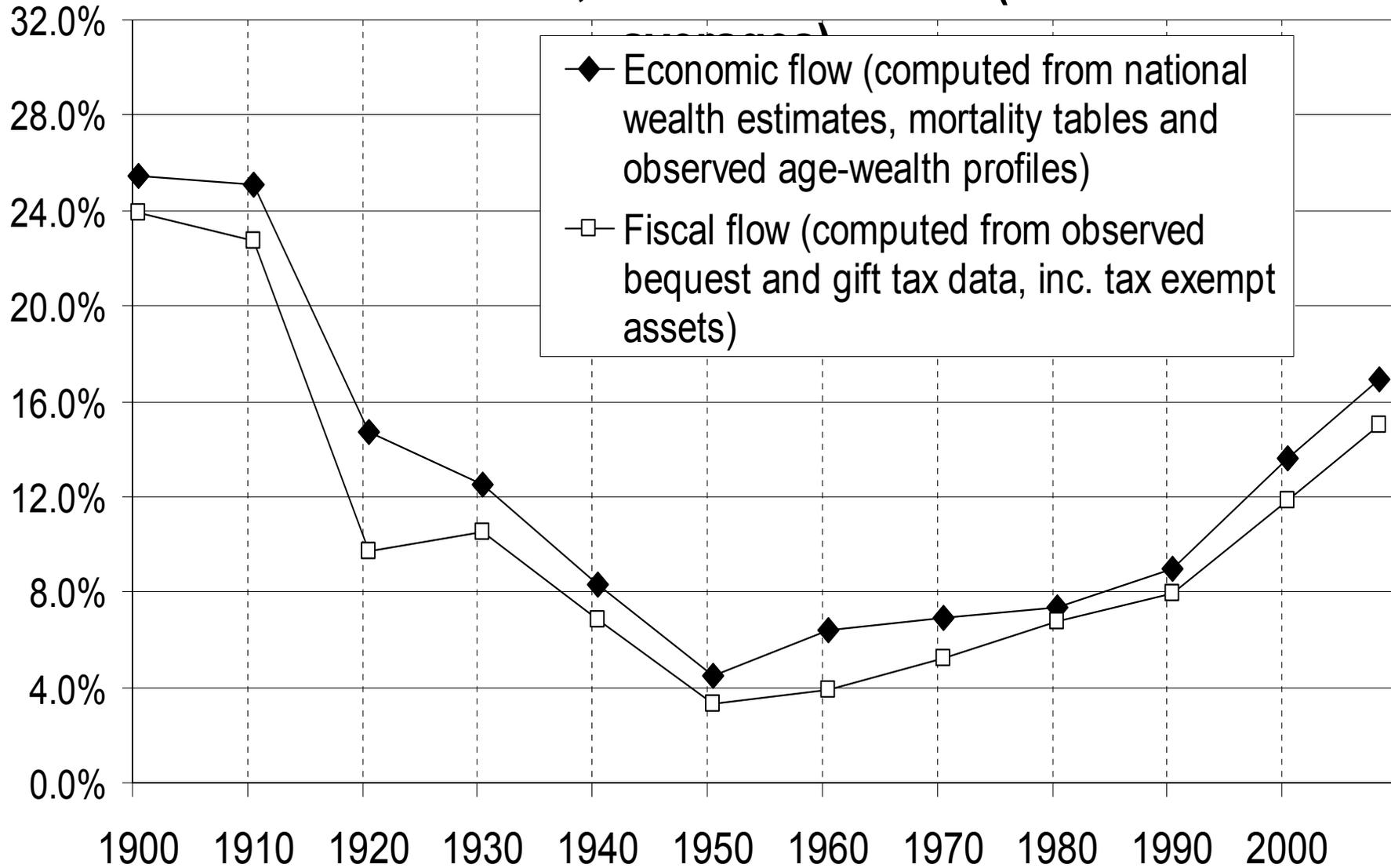
**On the Long-run
Evolution of Inheritance
France 1900-2050**

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- **There are two ways to become rich:** either through one's own work, or through inheritance
- In the 19th century and early 20th, it was obvious to everybody that the 2nd channel was important: inheritance and successors are everywhere in the literature, huge inheritance flow

- **Q:** Does this belong to the past? Did modern growth kill the inheritance channel? E.g. rise of human capital and meritocracy?
- This paper answers « **NO** » to this question and attempts to explain why, taking France 1900-2050 as an illustration: capital is back!

Figure 1: Annual inheritance flow as a fraction of national income, France 1900-2008 (decennial



What this paper does

- Documents and explains this fact
- Develops a simple simulation model reproducing this fact
- Applies the model to 2010-2050: we predict B/Y returns to 1900 level
- Applications to bequest wealth, lifetime inequality, and capital taxation

Application n°1: Modigliani-Summers controversy

- Modigliani AER 1986, JEP 1988: inheritance = 20% of total U.S. wealth accumulation
- Kotlikoff-Summers JPE 1981, JEP 1988: inheritance = 80% of total U.S. wealth accumulation
- Two problems: - Bad data
- **We do not live in a stationary world: life-cycle wealth was much more important in the 1950s-1970s than it is today**

Application n°2: lifetime inequality, labor vs capital

- Top incomes literature: Piketty JPE 2003, Piketty-Saez QJE 2003, Atkinson-Piketty OUP 2007 & 2010 → 23 countries.. but too descriptive, pb with capital side
 - Piketty-Postel-Vinay-Rosenthal AER 2006, « Wealth concentration in Paris 1807-1902 »
- **This paper = aggregate analysis, but building block for future work with heterogeneity and inequality**

Application n°3: socially-optimal capital taxation

- Economists have a pb with capital taxation: standard theory = optimal tax rate on all forms of capital and capital income = 0%
 - Very strong result: 0% capital tax rates are socially optimal for everybody, including for individuals and dynasties with zero wealth!
- ... But nobody seems to take it seriously:
nobody pushes for a complete suppression of corporate tax, property tax, estate tax, etc., i.e. 9.4% GDP tax revenue (EU25, Eurostat 2008)

- Atkinson-Stiglitz JPubE 1976: if wealth was entire life-cycle, no reason to tax capital
- I.e. differential commodity taxation is useless, redistributive labor taxation is sufficient: if $1+r =$ relative price of period 1 vs 2 consumption, no reason to overtax $C_2 = (1+r)(Y_L - C_1)$, just tax Y_L with $t(Y_L)$
- « If inequality is entirely labor-income-driven, no need to tax capital » = very intuitive and compelling argument for 0% capital tax

- ... except that life-cycle wealth plays a much less important role than what many economists tend to believe
- if bequest wealth is important, then the normative analysis is more complicated

→ **This paper = positive analysis, no normative model; but building block for future work on optimal capital taxation**

Data sources

- **Estate tax data:** tabulations by estate & age brackets 1902-1964; micro-files 1977-1984-1987-1994-2000-2006 (DMTG)
- **National wealth and income accounts:** Insee official series 1949-2009; linked up with various series 1900-1949 (Dugé, Colson, Divisia, Villa,..)
- **Wealth surveys:** Insee 1992-1998-2004

- French estate tax data is exceptionally good: universal, fully integrated bequest and gift tax since 1791
- Tax exempt assets: 15% in 1900s, 30%-35% in 2000s (life-insurance, unincorp.business & family firms,..)
- 350,000 estate tax returns/year in 1900s and 2000s, i.e. 65% of the 500,000 decedents (in 2000s, 20% of decedents pay tax, mostly people with no children; average tax rate <5%;top rate 40%-60%)

Computing inheritance flow

$$B_t/Y_t = \mu_t m_t W_t/Y_t$$

- W_t/Y_t = aggregate wealth/income ratio
 - m_t = aggregate mortality rate
 - μ_t = ratio between average wealth of decedents and average wealth of the living (= age-wealth profile)
- The U-shaped pattern of inheritance is the product of three U-shaped effects

Figure 2: Annual inheritance flow as a fraction of national income, France 1900-2008

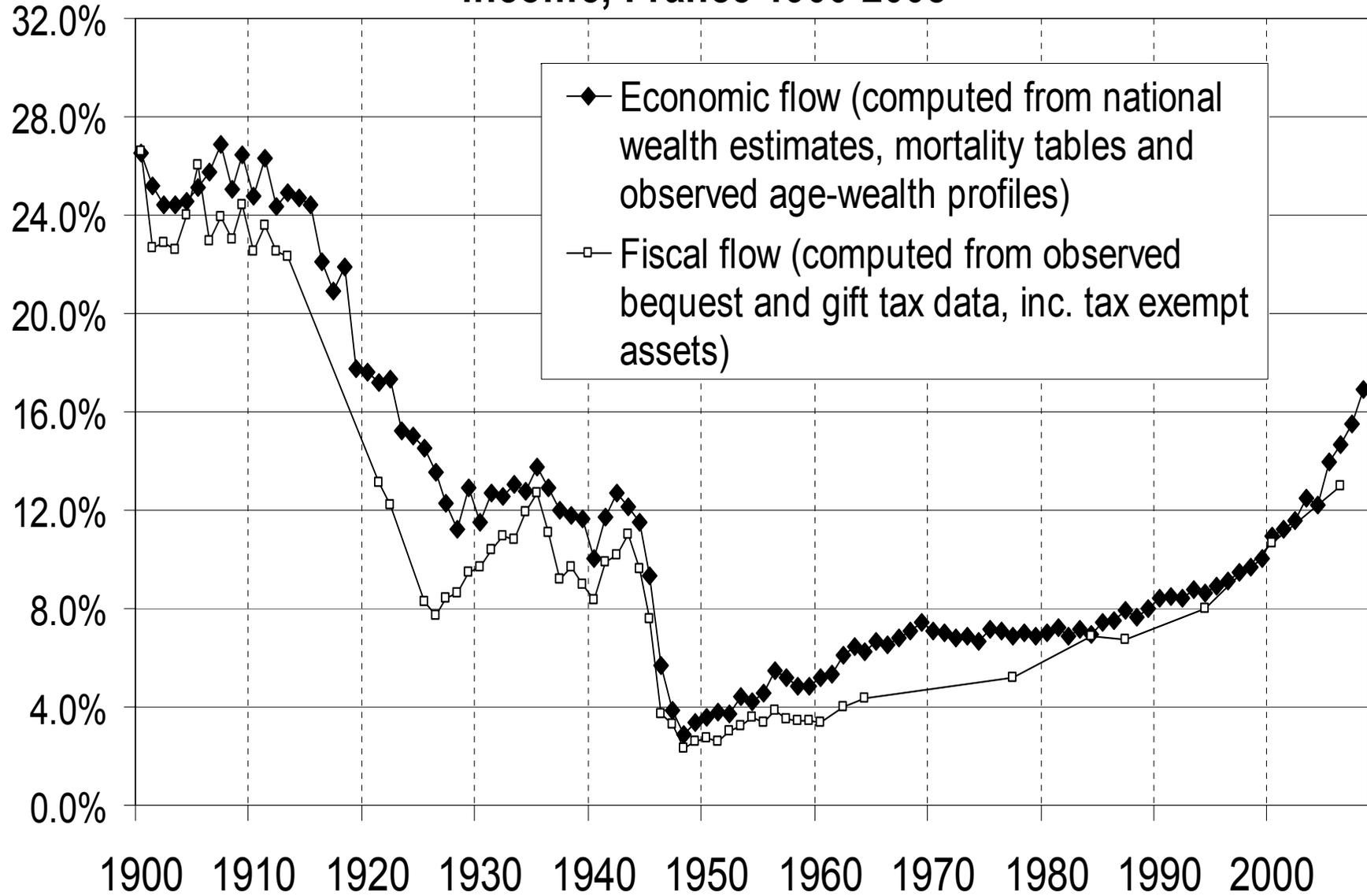
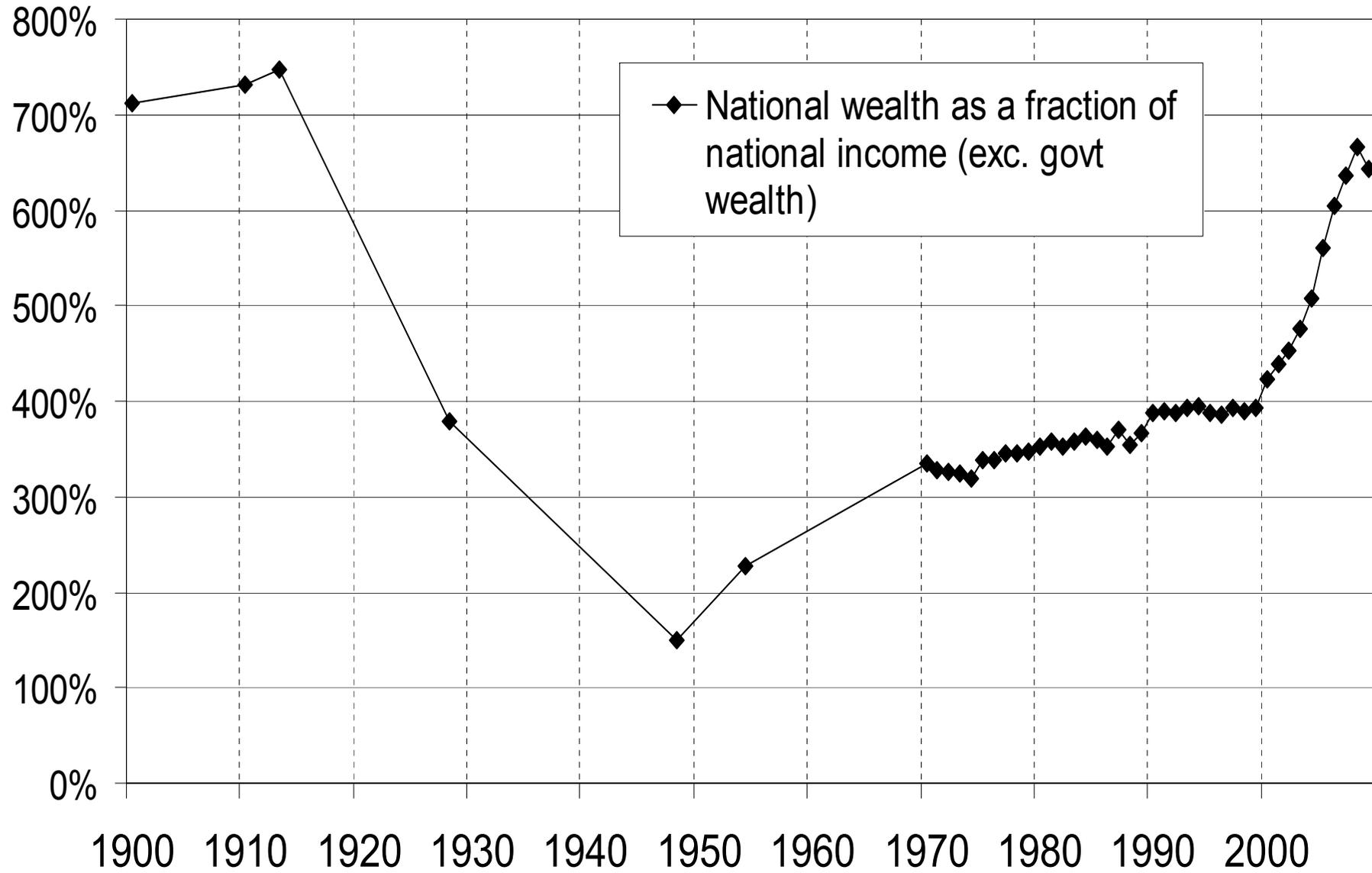


Figure 3: Wealth/income ratio in France 1900-2009



- 1900s: $Y = 30\text{-}35$ billions francs or, $W = 250$ billions, $B = 7.5\text{-}8.5$ billions
→ $W/Y = 700\%$, $B/Y = 25\%$
- 2009: $Y = 1\,500$ billions € (i.e. 25 000€ per capita), $W = 9\,000$ billions € (150 000€ per capita), $B = 230$ billions €
→ $W/Y = 600\%$, $B/Y = 15\%$
- Between 1900s and 1950s, W/Y divided by 2.5-3, B/Y divided by 5-6 → the fall in W/Y explains about half of the fall in B/Y

Figure 4: Mortality rate in France, 1900-2050

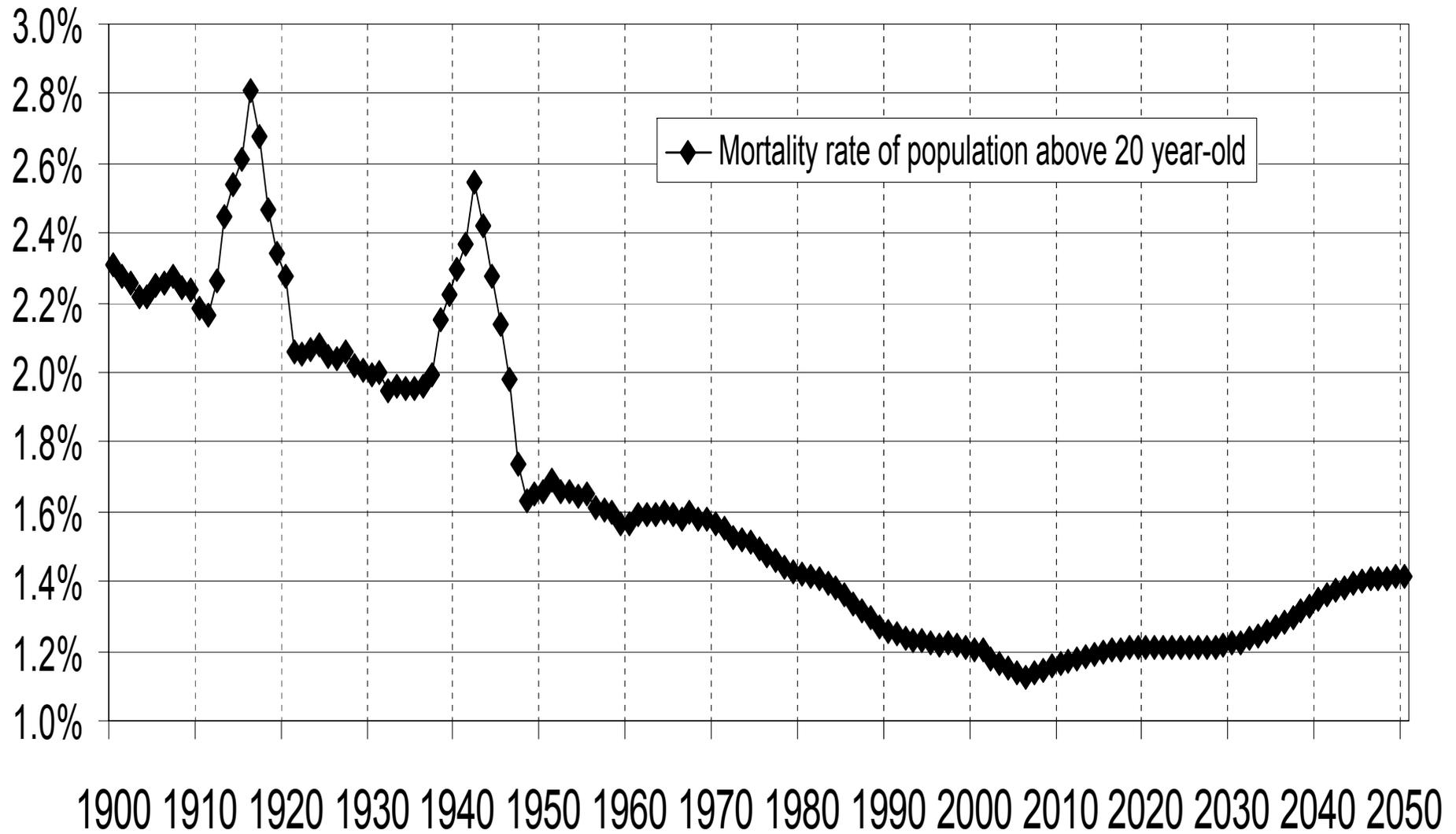
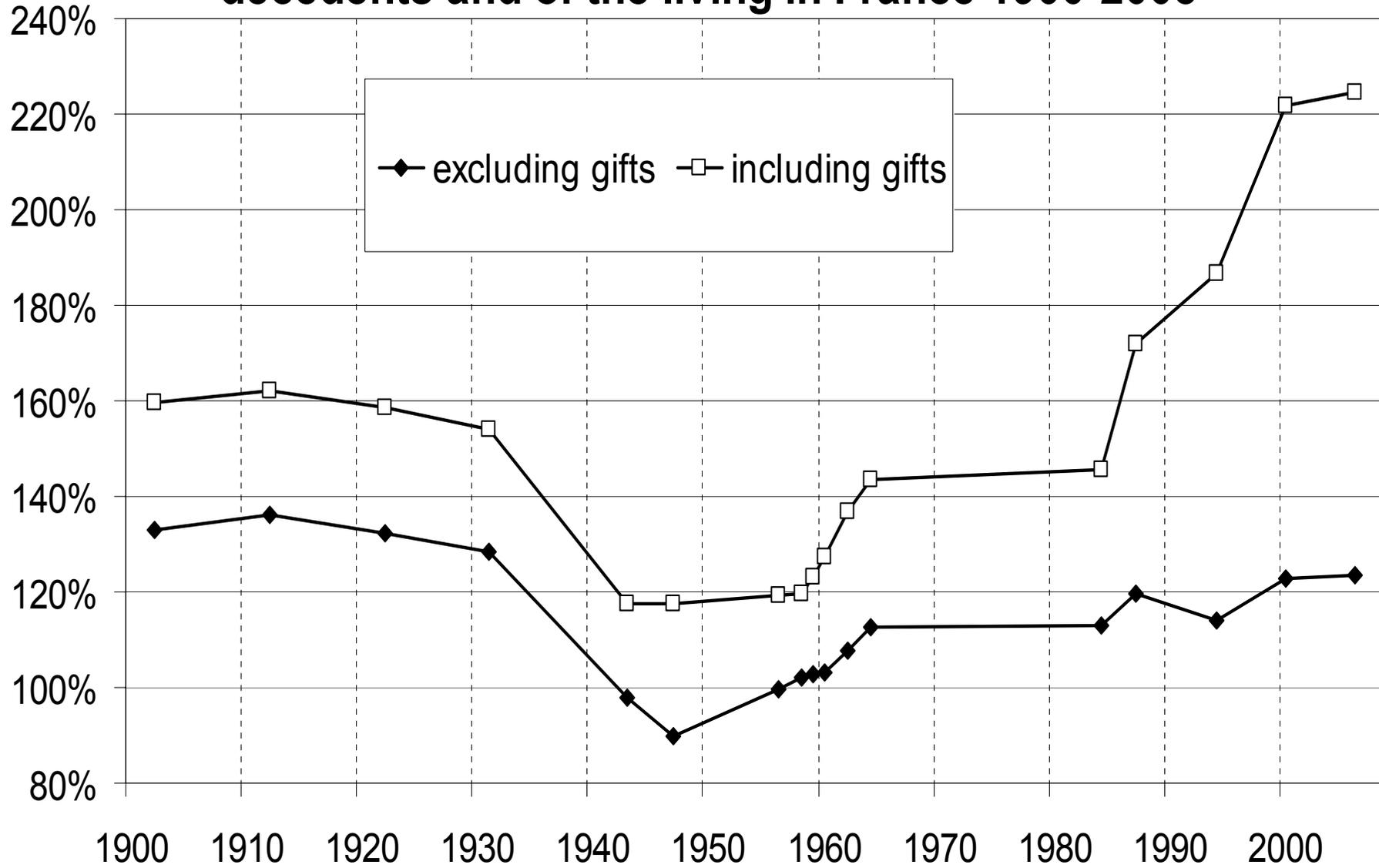


Figure 5: The ratio between average wealth of the decedents and of the living in France 1900-2008



How can we account for these facts?

- WW1 & 2 capital shocks played a major role, and it took a long time to recover
- Key question: why does the age-wealth profile become upward-sloping again? Clearly people don't annuitize
- **Key parameter: $r > g$ or $r < g$?**
- $r > g$ implies that old wealth matters a lot and upward-sloping profiles (for given savings behavior)

Simulations

- The observed dynamics of the age-wealth profile can be reproduced almost perfectly with a simple model based upon uniform savings rate across age groups, given observed r_t and g_t
- I start from the observed age-wealth profile $W_t(a)$ in 1900
- I take $Y_t = Y_{Lt} + Y_{Kt}$ from national accounts, and define $r_t = Y_{Kt}/W_t$

- I take $s_t = S_t/Y_t$ from national accounts, and assume uniform savings rates
- The transition equation for a given cohort is simply:

$$W_{t+1}(a+1) = W_t(a) + s_t [Y_{Lt}(a) + r_t W_t(a)]$$

- I apply observed mortality rates by age group, and observed age structure of heirs, donors and donees

Figure 6: Age of decedents vs heirs in France, 1900-2050

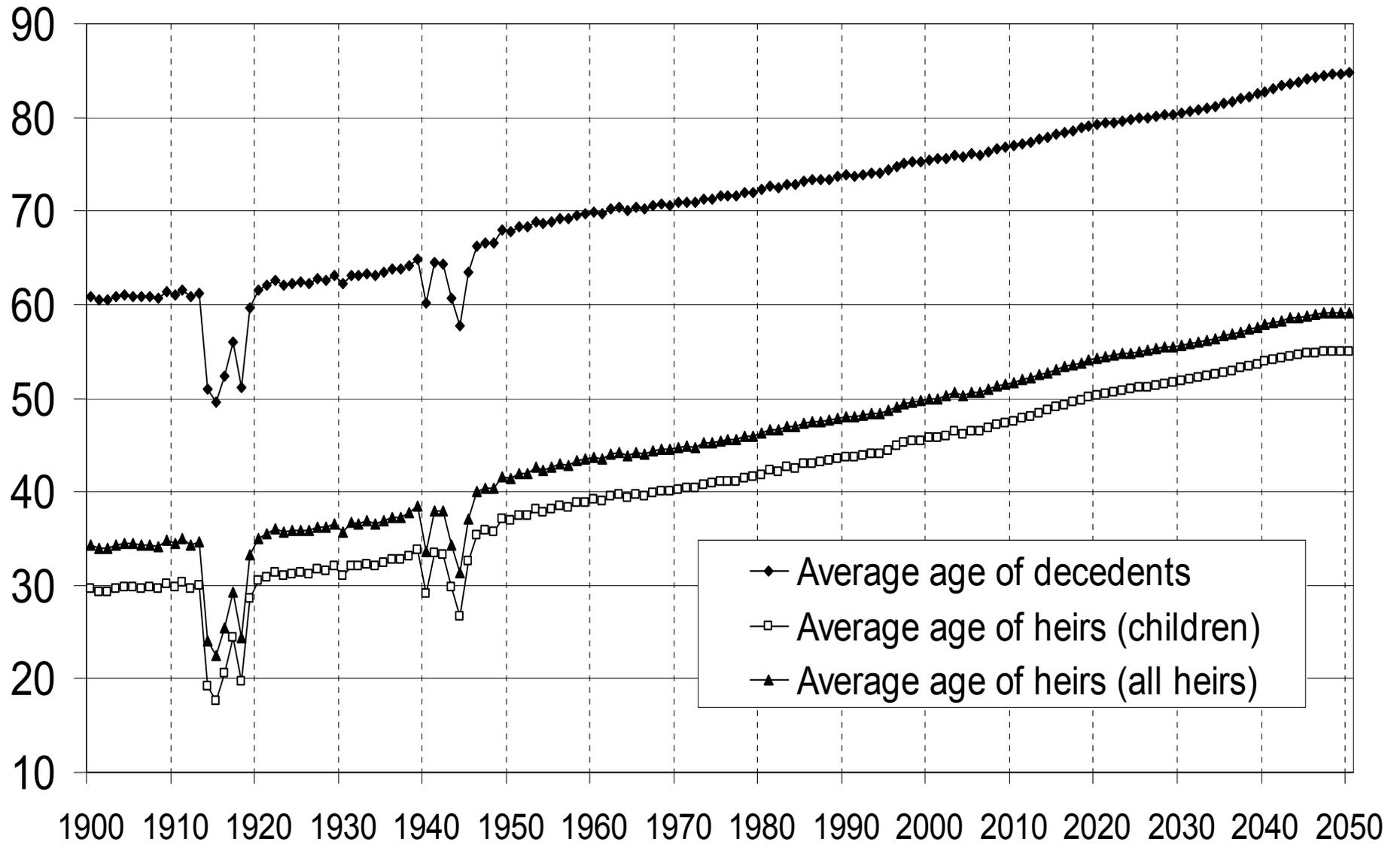
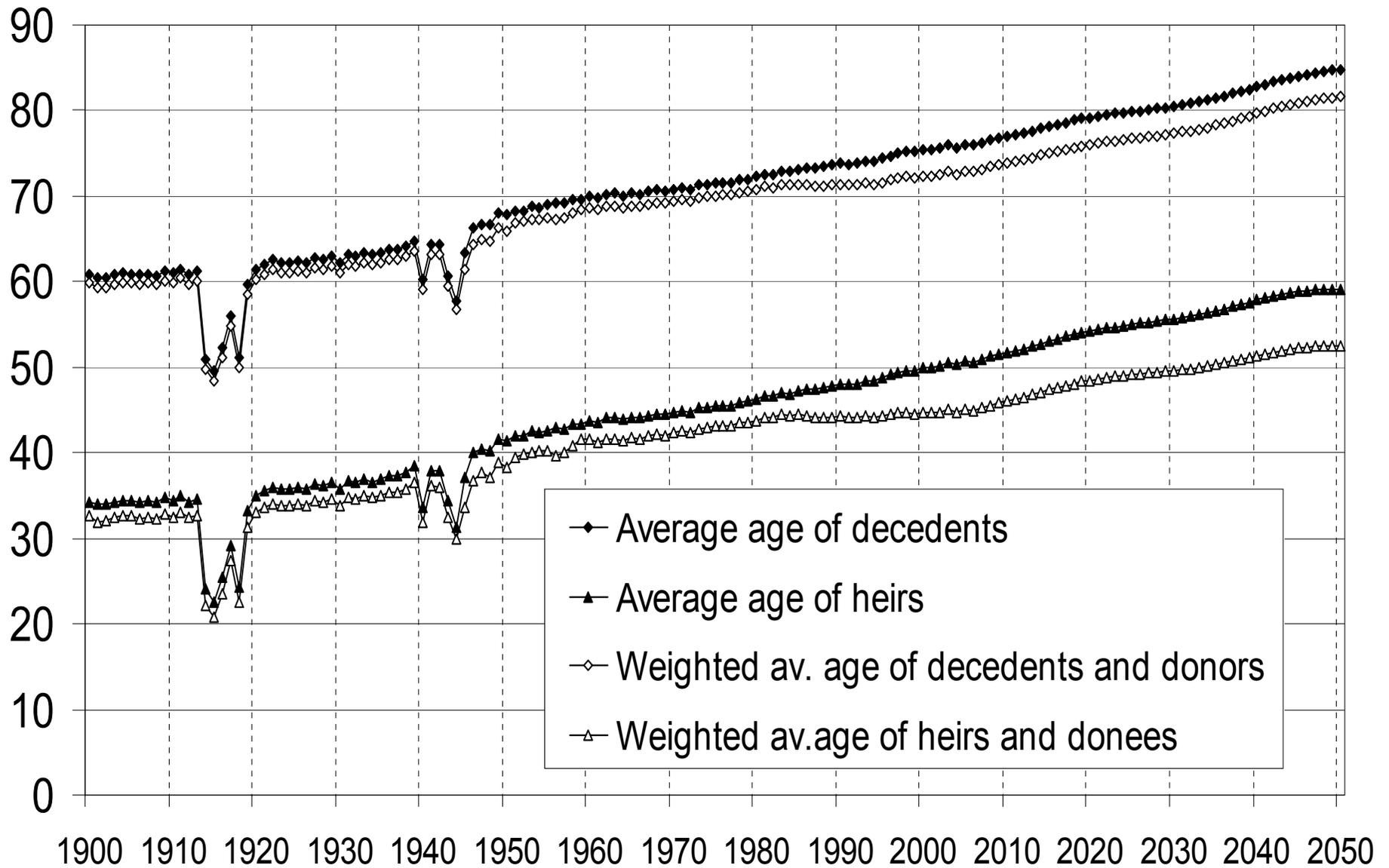
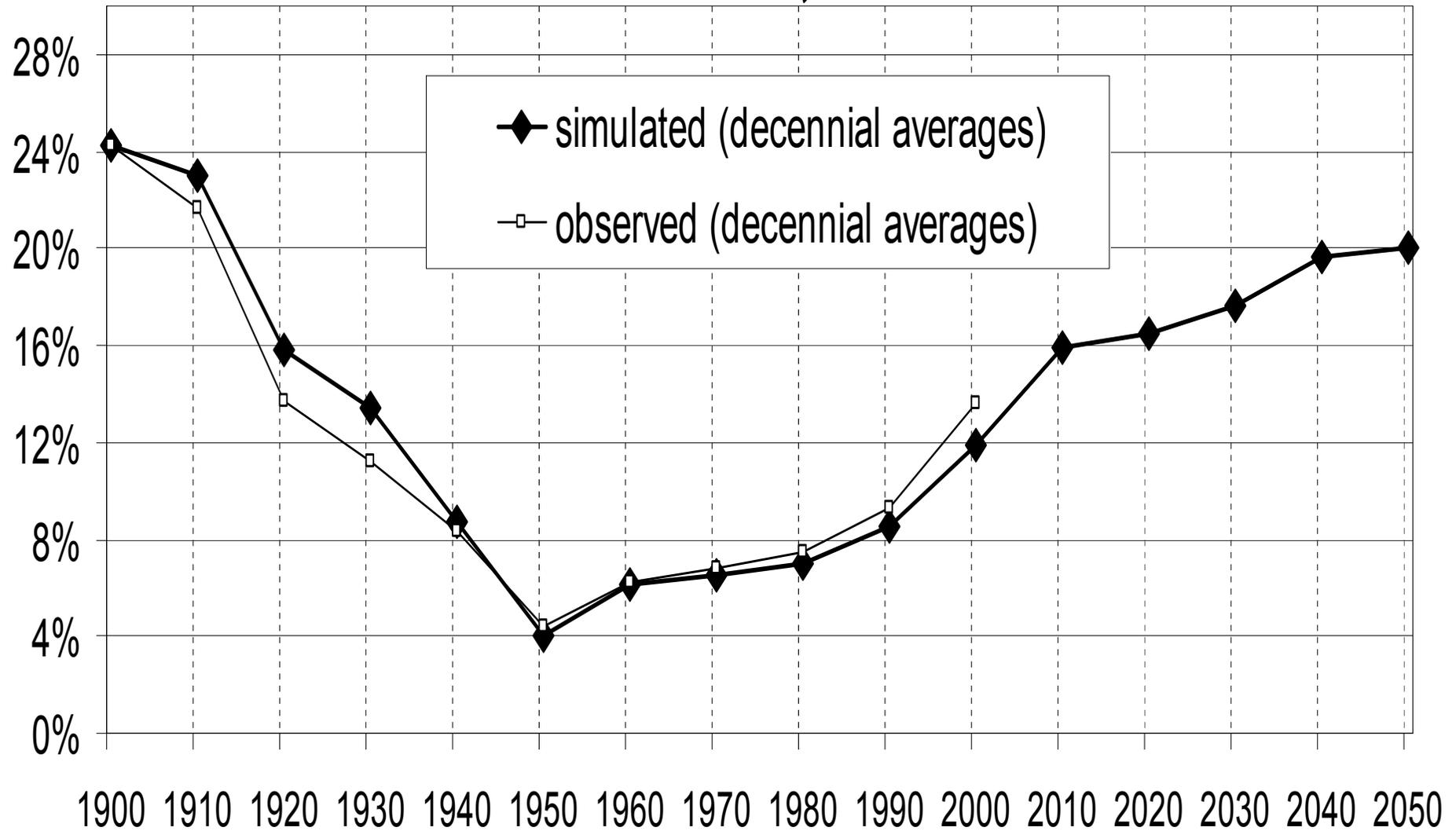


Figure 7: Age of givers vs receivers in France, 1900-2050



- 1900-1913: $r=4.1\%$, $g=1.4\%$
($W/Y=700\%$, $\alpha=28.5\%$, $s=10.2\%$)
- 1948-1978: $r=4.9\%$, $g=5.2\%$
($W/Y=278\%$, $\alpha=13.5\%$, $s=13.7\%$)
- 1978-2008: $r=4.2\%$, $g=1.8\%$
($W/Y=422\%$, $\alpha=17.9\%$, $s=11.1\%$)
*(exc. capital gains: 1978-2008: 2.1%
above CPI; 78-98 : 0.2%; 98-08 : 7.1%)*
- Simulations 2010-2050: **$r=4.0\%$** , **$g=2.0\%$**
($W/Y=600\%$, $\alpha=24\%$, $s=12\%$)

Figure 8: Simulations of annual inheritance flow as a fraction of national income, France 1900-2050



Some theory

- Why is B/Y around 20%-25% a magic number? What does it imply for W_B/W ?
- To simplify: deterministic demographic structure: everybody becomes adult at age A , has a kid at age P , inherits at age I , and dies at age D
- 1900: $A=20$, $P=30$, $D=60 \rightarrow I=D-H=30$
- 2050: $A=20$, $P=30$, $D=80 \rightarrow I=D-H=50$
- mortality rate: $m_t(20+) = 1/(D-A)$
(1900: about 2.5%; 2050: about 1.5%)

- $Y_t = F(K_t, H_t) = F(K_t, \exp(gt)L_t)$
- g = exogenous productivity growth rate
- E.g. Cobb-Douglas: $F(K,H) = K^\alpha H^{1-\alpha}$
- $Y_t = Y_{Kt} + Y_{Lt}$, with $Y_{Kt} = r_t K_t = \alpha_t Y_t$

- Define $\beta_t = K_t/Y_t =$ capital/output ratio
(= W_t/Y_t) (closed economy, no govt)
- Then $\alpha_t = r_t \beta_t$
- E.g. if $\beta_t = 600\%$, $r_t = 4\%$, then $\alpha_t = 24\%$

- Assume $S_t = sY_t = s_K Y_{Kt} + s_L Y_{Lt}$
 → Harrod-Domar steady-state: $sY = gK$
 i.e. $\beta^* = s/g$ (and $r^* = \alpha/\beta^*$)
 e.g. if $g=2\%$, $s=10\%$, then $\beta^* = 500\%$
- Dynastic model: $U = \int \exp(-\theta t) C_t^{1-\sigma}/(1-\sigma)$
 → Ramsey steady-state: $r^* = \theta + \sigma g$
- In effect: $s_L^* = 0\%$, $s_K = g/r^*\%$
- Intuition: Y_{Lt} grows at rate g , workers don't need to save; but capitalists need to save a fraction $g/r\%$ of $Y_{Kt} = r_t W_t$, so that W_t grows at rate g

- What about $b_t = B_t/Y_t = \mu_t m_t \beta_t$?
- If $s_L=0\%$, then the age-wealth profile $W_t(a)$ is very simple:
 - If $a < l$, then $W_t(a) = 0$
 - If $a \geq l$, then $W_t(a) = W_t$ (growing at rate g)
 - $\mu = 1/[(D-l)/(D-A)] = (D-A)/(D-l) > 100\%$
(1900: $\mu = 40/30 = 133\%$; 2050: $\mu = 60/30 = 200\%$)
 - since $m = 1/(D-A)$, **$b^* = \beta^*/(D-l)$**
- **I.e. if $\beta^* = 600\%$, $D-l = 30$, then $b^* = 20\%$,
irrespective of life expectancy D**

- More generally, take any s_L, s_K ; then:

Proposition 1: In steady-state:

(i) $\mu = (1 - \exp[-(g - s_K r)(D - A)]) / (1 - \exp[-(g - s_K r)(D - I)])$

(ii) If $s_K = g/r$, then $\mu = (D - A) / (D - I)$

(iii) More generally, $\mu > 100\%$, $\mu'(r) > 0$, $\mu'(g) < 0$

→ steady-state inheritance flow $b = \mu\beta / (D - A)$
rises with r and declines with g

Proposition 2: In steady-state, corrected capital share α^* = weighted average between b and α

From bequest flow to bequest wealth

- W_{Bt} = capitalized bequest wealth at time t
- $W_{Bt} / Y_t = \int_{s < t} B_{st} / Y_s \exp(r_{st} - g_{st}) ds$
- B_{st} = bequests received at time s by individuals alive at time t
- r_{st} = cumulated return to capital between time s and time t
- g_{st} = cumulated growth rate between time s and time t

- Deterministic demographic structure:

$$B_{st} = B_s \text{ for } t-(D-l) < s < t, \quad B_{st} = 0 \text{ for } s < t-(D-l)$$

$$\rightarrow \mathbf{W_B/Y = B/Y (exp[(r-g)(D-l)]-1) / (r-g)}$$

- Combined with $B/Y = \mu m W/Y$, one gets a simple formula for inheritance share in total wealth accumulation :

$$\rightarrow \mathbf{W_B/W = \mu m (exp[(r-g)(D-l)]-1) / (r-g)}$$

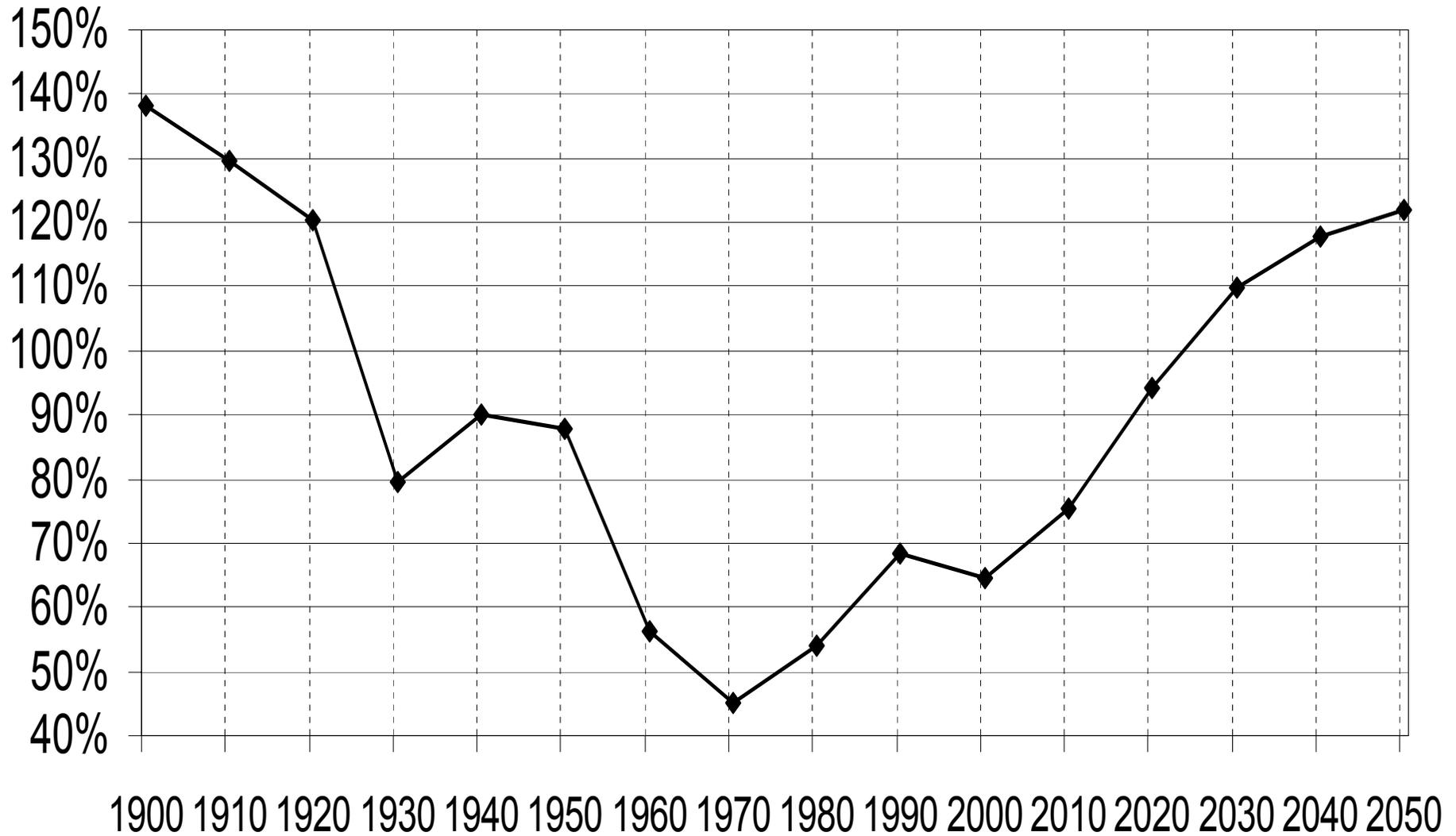
$$\rightarrow \text{if } r-g=0\%, \text{ then } W_B/W = \mu m (D-l)$$

$$\text{If } \mu=200\%, m=1.5\%, D-l=30: \mathbf{W_B/W=90\%}$$

$$\mathbf{\text{But if } r-g=2\%, \text{ then } W_B/W=123\%;}$$

$$\mathbf{\text{if } r-g=4\%, \text{ then } W_B/W=174\%}$$

Figure 9: The share of capitalized bequests in aggregate wealth accumulation France 1900-2050



Application to lifetime inequality

- 1900s: Top 1% = 50% of wealth; Top 10% = 90%; Bottom 50% = 0%-5%
 - 2000s: Top 1% = 20% of wealth; Top 10% = 50%; Bottom 50% = 5%-10%
- B/Y might return to 20%-25%, but wealth concentration still much lower than 1900
- ... except that $(\text{net } Y_{\perp})/Y$ is now much smaller than in 1900: one needs to introduce taxes and transfers

**Figure 10: Labor income share in national income, France
1900-2008**

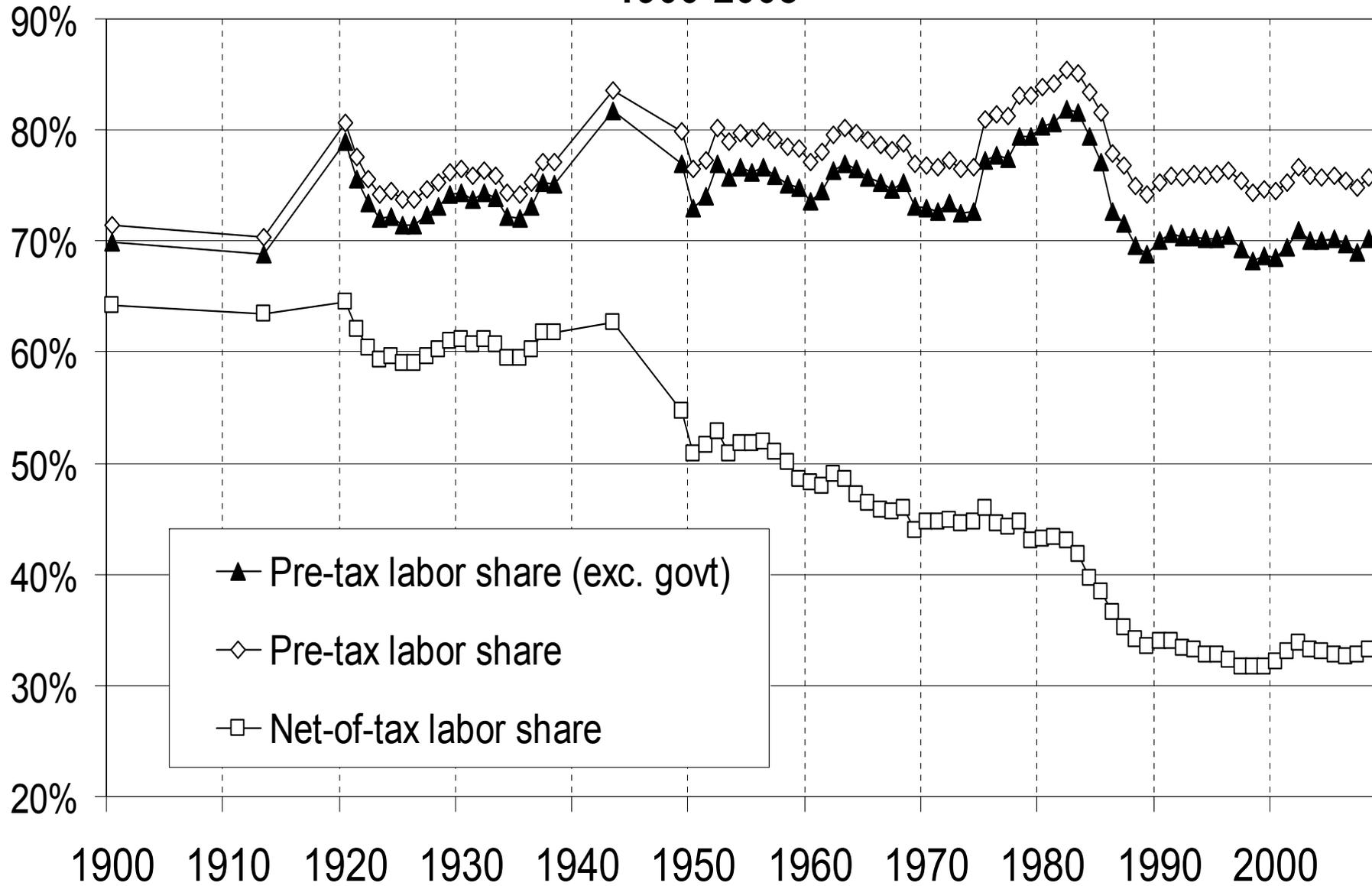
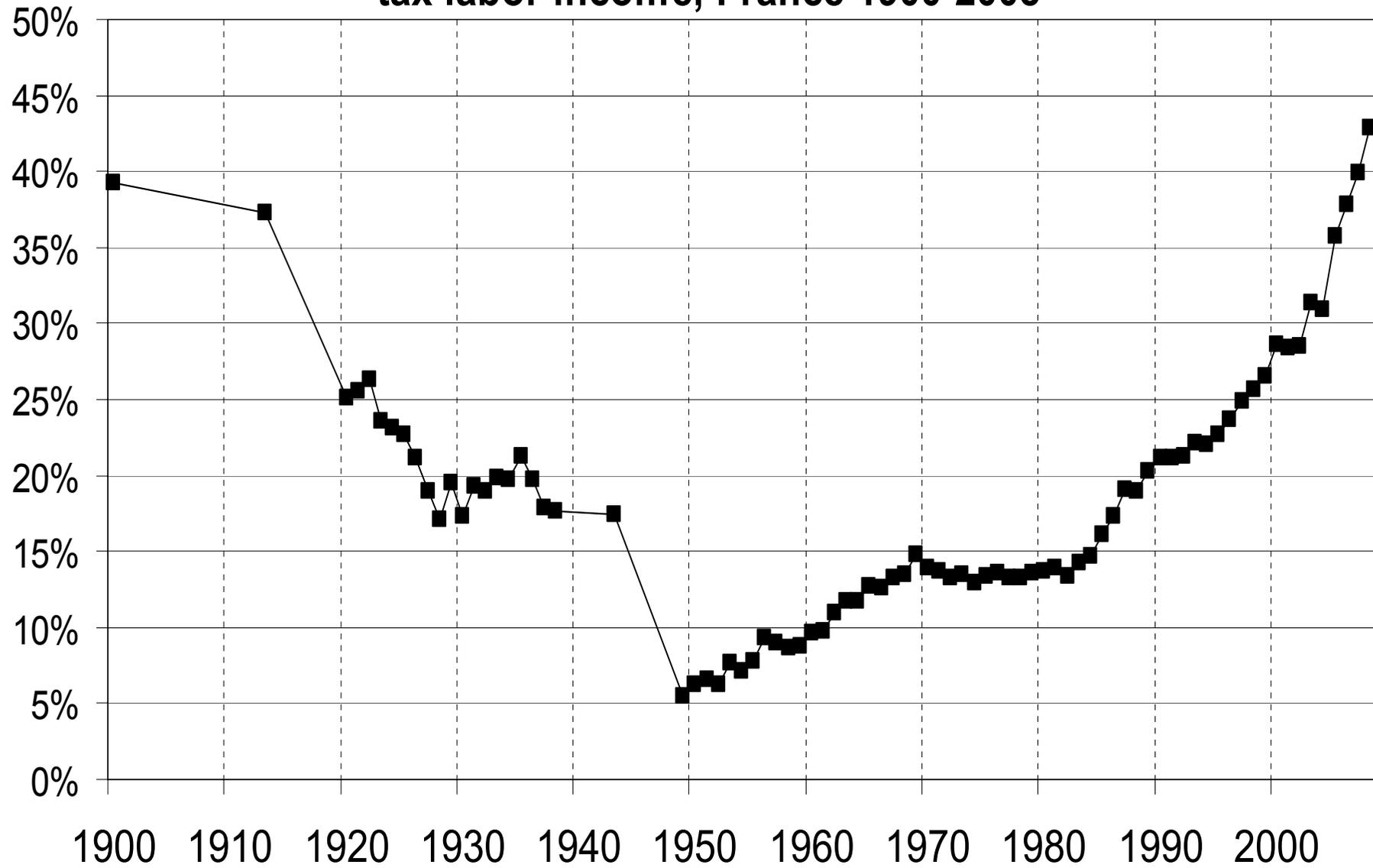


Figure 11: Annual inheritance flow as a fraction of net-of-tax labor income, France 1900-2008



What have we learned?

- Inheritance is likely to be a big issue in the 21st century
- Modern economic growth did not kill inheritance; the rise of human capital and meritocracy simply did not happen
- But no normative model... and life-cycle saving still exists: huge heterogeneity in savings behavior across individuals

- Main lesson: capital accumulation takes time... one should not look at the past 10 or 20 yrs and believe this is steady-state...
- Predictions: a lot depends on r vs $g+n$
 - China/India: inheritance doesn't matter
 - US: inheritance smaller than in France
 - Italy, Spain, Germany ($n < 0$): U-shaped pattern even bigger than France
 - world, very long run: $g+n=0\%$ (global warming): inheritance and past capital will dominate everything; back to Marx